

Single Body Analysis #5

$$\cancel{T_{1,2}} - m_1 g = m_1 a$$

$$\cancel{T_{2,3}} - \cancel{T_{1,2}} = m_2 a$$

$$\cancel{T_{3,4}} - \cancel{T_{2,3}} = m_3 a$$

$$m_4 g - \cancel{T_{3,4}} = m_4 a$$

$$m_4 g - m_1 g = m_1 a + m_2 a + m_3 a + m_4 a$$

$$m_4 g - m_1 g = (m_1 + m_2 + m_3 + m_4) a$$

$$a = \frac{m_4 g - m_1 g}{m_1 + m_2 + m_3 + m_4}$$

$$m_4 g - T_{3,4} = m_4 a$$

$$T_{3,4} = m_4 g - m_4 a$$

Single Body Analysis #5 (continued)

$$T_{3,4} - T_{2,3} = m_3 a$$

$$T_{2,3} = T_{3,4} - m_3 a$$

$$T_{1,2} - m_1 g = m_1 a$$

$$T_{1,2} = m_1 a + m_1 g$$

Var	Given value	Units	Description
g	10	$\frac{\text{m}}{\text{s}^2}$	Acceleration due to gravity
m_1	30	kg	Mass 1
m_2	20	kg	Mass 2
m_3	35	kg	Mass 3
m_4	60	kg	Mass 4

Single Body Analysis #5 (continued)

a		$\frac{\text{m}}{\text{s}^2}$	Acceleration
$T_{1,2}$		N	Tension 1
$T_{2,3}$		N	Tension 2
$T_{3,4}$		N	Tension 3

$$\begin{aligned}
 a &= \frac{m_4 g - m_1 g}{m_1 + m_2 + m_3 + m_4} \\
 &= \frac{(60 \text{ kg}) \left(10 \frac{\text{m}}{\text{s}^2}\right) - (30 \text{ kg}) \left(10 \frac{\text{m}}{\text{s}^2}\right)}{(30 \text{ kg}) + (20 \text{ kg}) + (35 \text{ kg}) + (60 \text{ kg})} \\
 &= 2.068965517 \frac{\text{m}}{\text{s}^2} \quad \checkmark
 \end{aligned}$$

Single Body Analysis #5 (continued)

$$\begin{aligned}T_{1,2} &= m_1 a + m_1 g \\&= (30 \text{ kg}) \left(2.068965517 \frac{\text{m}}{\text{s}^2} \right) + (30 \text{ kg}) \left(10 \frac{\text{m}}{\text{s}^2} \right) \\&= 362.0689655 \text{ N} \quad \checkmark\end{aligned}$$

$$\begin{aligned}T_{3,4} &= m_4 g - m_4 a \\&= (60 \text{ kg}) \left(10 \frac{\text{m}}{\text{s}^2} \right) - (60 \text{ kg}) \left(2.068965517 \frac{\text{m}}{\text{s}^2} \right) \\&= 475.8620690 \text{ N} \quad \checkmark\end{aligned}$$

$$\begin{aligned}T_{2,3} &= T_{3,4} - m_3 a \\&= (475.8620690 \text{ N}) - (35 \text{ kg}) \left(2.068965517 \frac{\text{m}}{\text{s}^2} \right) \\&= 403.4482759 \text{ N} \quad \checkmark\end{aligned}$$