

Centripetal Net Force Particle Model: Circular Motion Problem Solving Tips

When we did Newton's 2nd law, we established: sum of forces = net force = ma

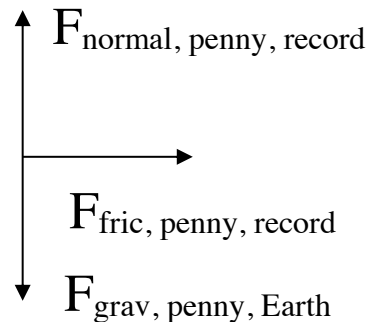
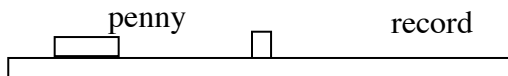
$$\Sigma F = m * a$$

Now, for circular motion: sum of radial forces = centripetal force = $\frac{mv^2}{r}$ $\Sigma F_C = m * a_c$

Note that "Centripetal force" is just a fancy name for the **net force**. It is not a kind of interaction (like gravity or normal forces) and is **NOT** drawn on force diagrams.

EXAMPLES:

1. What frictional force is needed to keep a penny from sliding off a record rotating at $33 \frac{1}{3}$ revolutions per minute when it is placed 10 cm from the center of the record. (mass of penny = 2.5 grams)



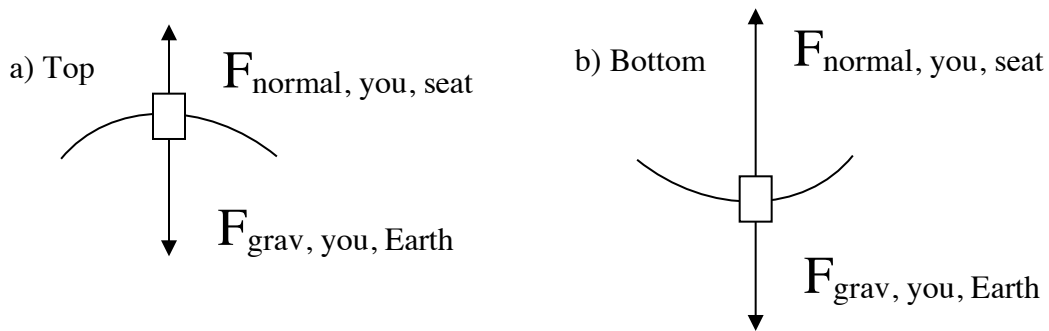
Net radial force = F_{fric}

$$33 \frac{1 \text{ rev}}{3 \text{ min}} * \frac{1 \text{ min}}{60 \text{ sec}} = 0.555 \frac{\text{rev}}{\text{s}} \quad \left(0.555 \frac{\text{rev}}{\text{s}}\right)^{-1} = 1.8 \text{ s/rev}$$

$$\Sigma F_C = F_{\text{fric}} = m * a_c \quad a_c = \frac{v^2}{r} \quad v = \frac{2\pi r}{T}$$

$$F_{\text{fric}} = m * \frac{\left(\frac{2\pi r}{T}\right)^2}{r} = 0.0025 \text{ kg} * \frac{\left(\frac{2\pi * 0.1 \text{ m}}{1.8 \text{ s}}\right)^2}{0.1 \text{ m}} =$$

2. A ferris wheel with a 20 m radius and tangential speed of 4 m/s has all 70 kg of you riding it. How big is the normal force exerted on you at **a)** the top **b)** the bottom?



Towards the center is positive

$$\Sigma F_{C\ Top} = m * a_c$$

$$F_g - F_N = m * \frac{v^2}{r}$$

$$F_N = F_g - m * \frac{v^2}{r}$$

$$\Sigma F_{C\ Bottom} = m * a_c$$

$$F_N - F_g = m * \frac{v^2}{r}$$

$$F_N = F_g + m * \frac{v^2}{r}$$