AP[°]

AP[®] Physics C: Mechanics 2013 Free-Response Ouestions

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TABLE OF INFORMATION DEVELOPED FOR 2012

CONSTANTS AND CONVERSION FACTORS							
Proton mass, $m_p = 1.67 \times 10^{-27}$ kg	Electron charge magnitude, $e = 1.60 \times 10^{-19} \text{ C}$						
Neutron mass, $m_n = 1.67 \times 10^{-27}$ kg	1 electron volt, 1 eV = 1.60×10^{-19} J						
Electron mass, $m_e = 9.11 \times 10^{-31}$ kg	Speed of light, $c = 3.00 \times 10^8 \text{ m/s}$						
Avogadro's number, $N_0 = 6.02 \times 10^{23} \text{ mol}^{-1}$	Universal gravitational constant, $G = 6.67 \times 10^{-11} \text{ m}^3/\text{kg} \cdot \text{s}^2$						
Universal gas constant, $R = 8.31 \text{ J/(mol}\cdot\text{K})$	Acceleration due to gravity at Earth's surface, $g = 9.8 \text{ m/s}^2$						
Boltzmann's constant, $k_B = 1.38 \times 10^{-23} \text{ J/K}$							
1 unified atomic mass unit,	$1 \text{ u} = 1.66 \times 10^{-27} \text{ kg} = 931 \text{ MeV}/c^2$						
Planck's constant,	$h = 6.63 \times 10^{-34}$ J·s = 4.14×10^{-15} eV·s						
	$hc = 1.99 \times 10^{-25} \text{ J} \cdot \text{m} = 1.24 \times 10^3 \text{ eV} \cdot \text{nm}$						
Vacuum permittivity,	$\boldsymbol{\epsilon}_0 = 8.85 \times 10^{-12} \text{ C}^2/\text{N} \cdot \text{m}^2$						
Coulomb's law constant,	$k = 1/4\pi\epsilon_0 = 9.0 \times 10^9 \text{ N} \cdot \text{m}^2/\text{C}^2$						
Vacuum permeability,	$\mu_0 = 4\pi \times 10^{-7} \ (\text{T-m})/\text{A}$						
Magnetic constant,	$k' = \mu_0 / 4\pi = 1 \times 10^{-7} \text{ (T-m)/A}$						
1 atmosphere pressure,	$1 \text{ atm} = 1.0 \times 10^5 \text{ N/m}^2 = 1.0 \times 10^5 \text{ Pa}$						

	meter,	m	mole,	mol	watt,	W	farad,	F
	kilogram,	kg	hertz,	Hz	coulomb,	С	tesla,	Т
UNII SVMBOLS	second,	S	newton,	Ν	volt,	V	degree Celsius,	°C
SIMDOLS	ampere,	А	pascal,	Pa	ohm,	Ω	electron-volt,	eV
	kelvin,	Κ	joule,	J	henry,	Н		

PREFIXES					
Factor	Prefix	Symbol			
10 ⁹	giga	G			
10^{6}	mega	М			
10 ³	kilo	k			
10^{-2}	centi	с			
10^{-3}	milli	m			
10^{-6}	micro	μ			
10^{-9}	nano	n			
10^{-12}	pico	р			

VALUES OF TRIGONOMETRIC FUNCTIONS FOR COMMON ANGLES								
θ	0°	30°	37°	45°	53°	60°	90°	
sin $ heta$	0	1/2	3/5	$\sqrt{2}/2$	4/5	$\sqrt{3}/2$	1	
$\cos\theta$	1	$\sqrt{3}/2$	4/5	$\sqrt{2}/2$	3/5	1/2	0	
tan $ heta$	0	$\sqrt{3}/3$	3/4	1	4/3	$\sqrt{3}$	~	

The following conventions are used in this exam.

- I. Unless otherwise stated, the frame of reference of any problem is assumed to be inertial.
- II. The direction of any electric current is the direction of flow of positive charge (conventional current).
- III. For any isolated electric charge, the electric potential is defined as zero at an infinite distance from the charge.

MECHANICS

$v = v_0 + at$	a = acceleration
1 2	F = force f = frequency
$x = x_0 + v_0 t + \frac{1}{2}at^2$	f = height
2	I = rotational inertia
$v^2 = v_0^2 + 2a(x - x_0)$	J = impulse
	K = kinetic energy
$\sum \mathbf{F} = \mathbf{F}_{net} = m\mathbf{a}$	k = spring constant
7	$\ell = \text{length}$
$\mathbf{F} = \frac{d\mathbf{p}}{d\mathbf{r}}$	L = angular momentum
dt	m = mass
$\mathbf{I} = \int \mathbf{F} dt = \Lambda \mathbf{p}$	N = normal force
$\mathbf{J} = \mathbf{J} \mathbf{F} a t = \Delta \mathbf{p}$	P = power
$\mathbf{n} - m\mathbf{v}$	p = momentum
$\mathbf{p} - m\mathbf{v}$	r = radius or distance
$F_{cuire} \leq uN$	\mathbf{r} = position vector
$fric = r^{2}$	T = period
$W = \int \mathbf{F} \cdot d\mathbf{r}$	t = time
" - Jrour	U = potential energy
1	v = velocity or speed
$K = \frac{1}{2}mv^2$	W = work done on a syst
2	x = position
D = dW	μ = coefficient of frictio
$r = \frac{1}{dt}$	θ = angle
	$\tau = \text{torque}$
$P = \mathbf{F} \cdot \mathbf{V}$	$\omega = $ angular speed
$\Delta U = m\sigma h$	$\alpha = angular acceleration$
Log mgn	ϕ – phase angle
u^2 2	φ = phase angle
$a_c = \frac{\sigma}{r} = \omega^2 r$	$\mathbf{F} = k\mathbf{y}$
,	$\mathbf{r}_{s} = -\kappa \mathbf{x}$
$\mathbf{\tau} = \mathbf{r} \times \mathbf{F}$	$1 1 2^{2}$
$\sum \sigma - \sigma = I \sigma$	$U_s = \frac{1}{2}kx$
$\Sigma \mathbf{t} = \mathbf{t}_{net} - T\mathbf{u}$	$u = u = \cos(\alpha t + \delta)$
$I = \int r^2 dm = \sum mr^2$	$x = x_{\max} \cos(\omega t + \varphi)$
$I = \int r \ am = \sum mr$	$T 2\pi 1$
$\Sigma = \frac{1}{2} \sum_{i=1}^{n} $	$I = \frac{1}{\omega} = \frac{1}{f}$
$\mathbf{r}_{cm} = \sum m\mathbf{r} / \sum m$	
$v = r\omega$	$T_s = 2\pi \sqrt{\frac{m}{L}}$
$\mathbf{I} = \mathbf{n} \times \mathbf{n} = I \mathbf{o}$	V K
$\mathbf{L} = \mathbf{r} \times \mathbf{p} = \mathbf{r} \boldsymbol{\omega}$	$T = 2\pi \frac{\ell}{\ell}$
$\mathbf{r} = 1$	$r_p = 2\pi \sqrt{g}$
$K = \frac{1}{2}I\omega^2$	Cm m
	$\mathbf{F}_G = -\frac{Gm_1m_2}{2}\hat{\mathbf{r}}$
$\omega = \omega_0 + \alpha t$	r ²
1	Gm_1m_2
$\theta = \theta_0 + \omega_0 t + \frac{1}{2}\alpha t^2$	$U_G = -\frac{r}{r}$
<u>-</u> _	

	$F = \frac{1}{4\pi\epsilon_0} \frac{q_1 q_2}{r^2}$	A = area B = magnetic field
	0	C = capacitance
	$\mathbf{E} = \frac{\mathbf{F}}{\mathbf{F}}$	d = distance
	q	E = electric field
	c 0	$\mathcal{E} = \mathrm{emf}$
	$\oint \mathbf{E} \cdot d\mathbf{A} = \frac{\mathbf{z}}{\epsilon_0}$	F = force
	-0	I = current
	$_{F}$ _ dV	J = current density
	$E = -\frac{1}{dr}$	L = inductance
	1 -	$\ell = \text{length}$
	$V = \frac{1}{4} \sum \frac{q_i}{q_i}$	n = number of loops of wire
	$4\pi\epsilon_0$ ${i}$ r_i	N = number of charge carriers
	1	per unit volume
	$U_E = qV = \frac{1}{4\pi \epsilon} \frac{q_1 q_2}{r_1}$	P = power
	$4\pi\epsilon_0$ r	O = charge
	0	a = point charge
	$C = \frac{\mathcal{L}}{V}$	R = resistance
	,	r = distance
am	$C = \frac{\kappa \epsilon_0 A}{1}$	t = time
CIII	$c = \frac{d}{d}$	U = potential or stored energy
m	$C = \Sigma C$	V = electric potential
/11	$C_p = \sum_i C_i$	v = velocity or speed
	1 1	ρ = resistivity
	$\frac{1}{C} = \sum \frac{1}{C}$	ϕ = magnetic flux
	$C_s = \frac{1}{i}C_i$	φ_m finagricule fran
1	dO	k = diffective constant
	$I = \frac{dE}{dt}$	
	1 1 .	$\oint \mathbf{B} \cdot d\boldsymbol{\ell} = \mu_0 I$
	$U_c = \frac{1}{2}QV = \frac{1}{2}CV^2$	$\int D d d \int \mu_0 d$
		$\mu_0 I d\ell \times \mathbf{r}$
	$R = \frac{\rho \ell}{\rho}$	$d\mathbf{B} = \frac{1}{4\pi} \frac{1}{r^3}$
	A	
	$\mathbf{E} = \rho \mathbf{J}$	$\mathbf{F} = \int I d\boldsymbol{\ell} \times \mathbf{B}$
	$I = Nev_d A$	$B_s = \mu_0 n I$
	V = IR	$\phi_m = \int \mathbf{B} \cdot d\mathbf{A}$
	$R_{s} = \sum_{i} R_{i}$	$\boldsymbol{\varepsilon} = \oint \mathbf{E} \boldsymbol{\cdot} d\boldsymbol{\ell} = -\frac{d\phi_m}{dt}$
	$\frac{1}{R_p} = \sum_i \frac{1}{R_i}$	$\boldsymbol{\varepsilon} = -L \frac{dI}{dt}$
	P = IV	$U_L = \frac{1}{2}LI^2$
	$\mathbf{F}_M = q\mathbf{v} \times \mathbf{B}$	2

ELECTRICITY AND MAGNETISM

GEOMETRY AND TRIGONOMETRY

A = area

b = base

h = height

 $\ell = \text{length}$

w = width

r = radius

V = volume

C = circumference

S = surface area

Rectangle A = bh

Triangle

 $A = \frac{1}{2}bh$

Circle

 $A = \pi r^2$

 $C = 2\pi r$

Rectangular Solid

 $V = \ell w h$

Cylinder

$$V = \pi r^2 \ell$$

$$S = 2\pi r\ell + 2\pi r^2$$

Sphere

$$V = \frac{4}{3}\pi r^3$$
$$S = 4\pi r^2$$

Right Triangle

$$a^{2} + b^{2} = c^{2}$$
$$\sin \theta = \frac{a}{c}$$
$$\cos \theta = \frac{b}{c}$$
$$\tan \theta = \frac{a}{b}$$



CALCULUS $\frac{df}{dx} = \frac{df}{du}\frac{du}{dx}$ $\frac{d}{dx}(x^n) = nx^{n-1}$ $\frac{d}{dx}(e^x) = e^x$ $\frac{d}{dx}(\ln x) = \frac{1}{x}$ $\frac{d}{dx}(\sin x) = \cos x$ $\frac{d}{dx}(\cos x) = -\sin x$ $\int x^{n} dx = \frac{1}{n+1} x^{n+1}, \, n \neq -1$ $\int e^x dx = e^x$ $\int \frac{dx}{x} = \ln|x|$ $\int \cos x \, dx = \sin x$ $\int \sin x \, dx = -\cos x$

2013 AP® PHYSICS C: MECHANICS FREE-RESPONSE QUESTIONS

PHYSICS C: MECHANICS SECTION II Time—45 minutes 3 Questions

Directions: Answer all three questions. The suggested time is about 15 minutes for answering each of the questions, which are worth 15 points each. The parts within a question may not have equal weight. Show all your work in this booklet in the spaces provided after each part.



Mech 1.

A student places a 0.40 kg glider on an air track of negligible friction and holds it so that it touches an uncompressed ideal spring, as shown in Figure 1 above. The student then pushes the glider back to compress the spring by 0.25 m, as shown in Figure 2. At time t = 0, the student releases the glider, and a motion sensor begins recording the velocity of the reflector at the front of the glider as a function of time. The data points are shown in the table below. At time t = 0.79 s, the glider losses contact with the spring.

Time (s)	0	0.25	0.50	0.75	1.00	1.50	2.00
Velocity (m/s)	0	0.25	0.43	0.48	0.50	0.49	0.51

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(a) On the axes below, plot the data points for velocity v as a function of time *t* for the glider, and draw a smooth curve that best fits the data. Be sure to label an appropriate scale on the vertical axis.



- (b) The student wishes to use the data to plot position x as a function of time t for the glider.
 - i. Describe a method the student could use to do this.
 - ii. On the axes below, sketch the position x as a function of time t for the glider. Explicitly label any intercepts, asymptotes, maxima, or minima with numerical values or algebraic expressions, as appropriate.



- (c) Calculate the time at which the glider makes contact with the bumper at the far right.
- (d) Calculate the force constant of the spring.
- (e) The experiment is run again, but this time the glider is attached to the spring rather than simply being pushed against it.
 - i. Determine the amplitude of the resulting periodic motion.
 - ii. Calculate the period of oscillation of the resulting periodic motion.

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Mech 2.

A box of mass *m* initially at rest is acted upon by a constant applied force of magnitude F_A , as shown in the figure above. The friction between the box and the horizontal surface can be assumed to be negligible, but the box is subject to a drag force of magnitude kv where v is the speed of the box and k is a positive constant. Express all your answers in terms of the given quantities and fundamental constants, as appropriate.

(a) The dot below represents the box. Draw and label the forces (not components) that act on the box.

- (b) Write, but do not solve, a differential equation that could be used to determine the speed v of the box as a function of time *t*. If you need to draw anything other than what you have shown in part (a) to assist in your solution, use the space below. Do NOT add anything to the figure in part (a).
- (c) Determine the magnitude of the terminal velocity of the box.
- (d) Use the differential equation from part (b) to derive the equation for the speed v of the box as a function of time *t*. Assume that v = 0 at time t = 0.
- (e) On the axes below, sketch a graph of the speed v of the box as a function of time *t*. Explicitly label any intercepts, asymptotes, maxima, or minima with numerical values or algebraic expressions, as appropriate.



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Note: Figure not drawn to scale.

Mech 3.

A disk of mass M = 2.0 kg and radius R = 0.10 m is supported by a rope of negligible mass, as shown above. The rope is attached to the ceiling at one end and passes under the disk. The other end of the rope is pulled upward with a force F_A . The rotational inertia of the disk around its center is $MR^2/2$.

(a) Calculate the magnitude of the force F_A necessary to hold the disk at rest.

At time t = 0, the force F_A is increased to 12 N, causing the disk to accelerate upward. The rope does not slip on the disk as the disk rotates.

- (b) Calculate the linear acceleration of the disk.
- (c) Calculate the angular speed of the disk at t = 3.0 s.
- (d) Calculate the increase in total mechanical energy of the disk from t = 0 to t = 3.0 s.
- (e) The disk is replaced by a hoop of the same mass and radius. Indicate whether the linear acceleration of the hoop is greater than, less than, or the same as the linear acceleration of the disk.

___Greater than ___Less than ___The same as

Justify your answer.

STOP

END OF EXAM